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PREFACE

This technical report describes the fifth generation Penn State/NCAR Mesoscale Model Version 1, or MM5V1. It is intended to provide scientific and technical documentation of the model for users. Source code documentation is available as a separate Technical Note (NCAR/TN-392) by Haagenson et al. (1994). Comments and suggestions for improvements or corrections, are welcome and should be sent to the authors.

(Last revision: June 1996)
ACKNOWLEDGMENTS

A large number of scientists, students, and sponsors, too numerous to mention, have made significant contributions towards developing and improving this model. We would like to thank everyone who directly implemented changes and corrections into the code, as well as everyone who helped to identify errors and problems.

We would also like to extend our gratitude to the two reviewers (Prof. Tom Warner, and Dr. Jian-Wen Bao), whose comments improved the manuscript significantly.

Computing for this model development was undertaken on the CRAY YMP at NCAR, which is supported by the National Science Foundation.

The writing of this technical document was in part supported by the Department of Energy through grant DEA105-90ER61070, and the California Air Resources Board through subcontract AG/990-TS05-S02 from Alpine Geophysics.